

**Quiz 7**  
**CHEM 325**  
**Spring 2009**

Name: \_\_\_\_\_

1. (6 Points) The molecule  $\text{CH}_2\text{Cl}_2$  belongs to the point group  $C_{2v}$ . The displacement vectors of the atoms span  $5 A_1 + 2 A_2 + 4 B_1 + 4 B_2$ . What are the symmetries of the normal modes?

**There are 9 normal modes ( $3N-6$  with  $N = 5$ ) for  $\text{CH}_2\text{Cl}_2$ .**

**Removing the translations ( $A_1 + B_1 + B_2$ ) leaves  $4 A_1 + 2 A_2 + 3 B_1 + 3 B_2$ .**

**Removing the rotations ( $A_2 + B_1 + B_2$ ) leaves  $4 A_1 + A_2 + 2 B_1 + 2 B_2$ , which are a total of 9 normal modes.**

| $C_{2v}$ | E | $C_2$ | $\sigma_v(xz)$ | $\sigma_v(yz)$ |          |                 |
|----------|---|-------|----------------|----------------|----------|-----------------|
| $A_1$    | 1 | 1     | 1              | 1              | z        | $x^2, y^2, z^2$ |
| $A_2$    | 1 | 1     | -1             | -1             | $R_z$    | xy              |
| $B_1$    | 1 | -1    | 1              | -1             | x, $R_y$ | xz              |
| $B_2$    | 1 | -1    | -1             | 1              | y, $R_x$ | yz              |

2. (4 Points) Will  $\text{Cl}_2$  ( $\tilde{\nu} = 559.7 \text{ cm}^{-1}$ ) or  $\text{Br}_2$  ( $\tilde{\nu} = 321.0 \text{ cm}^{-1}$ ) have a higher proportion of molecules in the first vibrational excited state at 300.0 K? Explain.

**The vibrational terms are  $G(v) = \left(v + \frac{1}{2}\right)\tilde{\nu}$ , assuming that we may treat these**

**molecules as simple harmonic oscillators, and the difference between the  $v = 0$  and**

**$v = 1$  states would be  $G(1) - G(0) = \left(1 + \frac{1}{2}\right)\tilde{\nu} - \left(0 + \frac{1}{2}\right)\tilde{\nu} = \tilde{\nu}$ . The Boltzmann**

**distribution predicts that states with higher energy will be less populated than states at lower energy at a given temperature. Since the splitting between the vibrational states is smaller for  $\text{Br}_2$  (since it has the smaller  $\tilde{\nu}$ ), there will be more  $\text{Br}_2$  molecules than  $\text{Cl}_2$  molecules in the first vibrational state at 300.0 K.**

3. (5 Points) The normal modes for CH<sub>4</sub> are A<sub>1</sub>, E, T<sub>2</sub> and T<sub>2</sub>. Which of these modes will be IR active (i. e., observable in an IR absorption spectrum) and which will be Raman active (i. e., observable in a Raman spectrum)?

**The symmetry of a normal mode must be the same as x, y, or z (the mode must transform as x, y or z) to be IR allowed, while a normal mode must transform as a quadratic to be Raman allowed.**

**From the character table we see that A<sub>1</sub>, E and both T<sub>2</sub> transform as quadratics, and are thus Raman allowed.**

**Both T<sub>2</sub> normal modes transform also transform as (x, y, z) and are thus allowed in IR.**

| T <sub>d</sub> | E | 8 C <sub>3</sub> | 3 C <sub>2</sub> | 6 S <sub>4</sub> | 6 σ <sub>d</sub> |   |   |
|----------------|---|------------------|------------------|------------------|------------------|---|---|
| A <sub>1</sub> | 1 | 1                | 1                | 1                | 1                |   | x <sup>2</sup> +y <sup>2</sup> +z <sup>2</sup>                                      |
| A <sub>2</sub> | 1 | 1                | 1                | -1               | -1               |   |   |
| E              | 2 | -1               | 2                | 0                | 0                |   | (2z <sup>2</sup> -x <sup>2</sup> -y <sup>2</sup> , x <sup>2</sup> -y <sup>2</sup> ) |
| T <sub>1</sub> | 3 | 0                | -1               | 1                | -1               | (R <sub>x</sub> , R <sub>y</sub> , R <sub>z</sub> ) |   |
| T <sub>2</sub> | 3 | 0                | -1               | -1               | 1                | (x, y, z)   | (xy, xz, yz)  |

4. (7 Points) The allowed vibrational transitions of a diatomic molecule occur at wavenumbers of  $\tilde{\nu} - 2(v+1)x_e\tilde{\nu}$ . A graph of the wavenumber of the first three vibrational transitions of NaI as a function of  $v+1$  yields a straight line with an intercept of 286.00 cm<sup>-1</sup> and a slope of -1.5000 cm<sup>-1</sup>. What is  $D_e$  (the depth of the Morse potential well)?

**The given equation is in the form of a straight line with a slope of  $-2x_e\tilde{\nu}$  and an**

**intercept of  $\tilde{\nu}$ . Therefore,  $x_e\tilde{\nu} = \frac{1.5000 \text{ cm}^{-1}}{2} = 0.75000 \text{ cm}^{-1}$ .**

**Rearrange  $x_e = \frac{\tilde{\nu}}{4D_e}$  to  $D_e = \frac{\tilde{\nu}}{4x_e} = \frac{\tilde{\nu}^2}{4x_e\tilde{\nu}}$ , and solve**

$$D_e = \frac{\tilde{\nu}^2}{4x_e\tilde{\nu}} = \frac{(286.00 \text{ cm}^{-1})^2}{4(0.75000 \text{ cm}^{-1})} = 27265.3 \text{ cm}^{-1}$$

**For NaI  $D_e$  is 27265. cm<sup>-1</sup>.**